Self–organization and multiscale approach: A mathematical theory

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A general class of mathematical structures (integro–differential equations) that models swarming behavior at the mesoscopic level is proposed. These structures lead to interesting mathematical problems of blow–up versus global existence ([2], [3]). Macroscopic ("hydrodynamic") limits are discussed ([4]). The corresponding individually–based (microscopic) model is proposed (cf. [1]).

References

[1] J. Banasiak, M. Lachowicz, Methods of small parameter in mathematical biology, Birkhäuser, Boston 2014.

[2] M. Lachowicz, H. Leszczyński, M. Parisot, A simple kinetic equation of swarm formation: blow-up and global existence, Appl. Math. Letters, 57, 2016, 104-107.

[3] M. Lachowicz, H. Leszczyński, M. Parisot, Blow–up and global existence for a kinetic equation of swarm formation, to appear.

[4] M. Parisot, M. Lachowicz, A kinetic model for the formation of swarms with nonlinear interactions, Kinetic Related Models, 9, 1, 131–164, 2016.