# EXAM FOR "ALGEBRAIC STRUCTURES" (6ALGS) SUMMER SEMESTER 2023/2024

## QUESTIONS SET NO. 8

#### 1.

Formulate and prove the second and third homomorphism theorems for algebras.

### 2.

Is it true that any group satisfying the condition

- a)  $x^2 = 1$
- b)  $x^3 = 1$

for any element *x* of the group, is abelian?

#### **3.**

Give example of a group whose group of inner automorphisms is isomorphic to  $\mathbb{Z}/2\mathbb{Z}$ , and the group of all automorphisms is isomorphic to  $\mathbb{Z}/3\mathbb{Z}$ .